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Exam #2, October 28, Calculus I, Fall, 2006, W. Stephen Wilson

I agree to complete this exam without unauthorized assistance from any person, materials or device.

Name: \_\_\_\_\_ Date: \_\_\_\_\_

TA Name and section: \_\_\_\_\_

**NO CALCULATORS, NO PAPERS, SHOW WORK.** (60 points total)

The  $\sin^2(u)$  isn't particularly important in these first problems. The function  $f(x)$  is always assumed to be continuous.

1. (3 points) Compute  $\frac{d}{dx} \int_0^x \sin^2(u) du$ .

2. (3 points) Compute  $\frac{d}{dx} \int_0^{x^2} \sin^2(u) du$ .

3. (3 points) Compute  $\frac{d}{dx} \int_{x^2}^0 \sin^2(u) du$ .

4. (3 points) Compute  $\frac{d}{dx} \int_{x^2}^{x^3} \sin^2(u) du$ .

5. (3 points) Compute  $\int_0^1 \frac{dx}{1+x^2}$ .

6. (3 points) Find the area under one hump of the curve  $y = \sin(x)$ .

7. (3 points) What is the average value of one hump of  $\sin(x)$ ?

8. (3 points) What is  $\int x^n dx$  for  $n \neq -1$ ?

9. (3 points) What is  $\int \frac{dx}{x}$ ?

10. (3 points) What is  $\int \frac{dx}{\sqrt{x}}$ ?

11. (3 points) What is  $\int \cos(2x)dx$ ?

**12.** (3 points) If  $f(x) > 0$ , what is the integral for the area under  $f$  and above the  $x$ -axis from  $a$  to  $b$ ,  $a < b$ ?

**13.** (3 points) If  $f(x) > 0$ , what is the integral for the volume of the solid of revolution obtained by rotating the area under  $f$  and above the  $x$ -axis from  $a$  to  $b$ ,  $a < b$  about the  $x$ -axis?



14. (3 points) What is the area trapped between the function  $f(x)$  and the  $x$ -axis between  $a$  and  $d$ ,  $a < d$ .

15. (3 points) Set up the integral for the area inside a circle of radius  $a$ . (Do not try to integrate it.)

16. (3 points) What is the integral for the length of the curve  $y = f(x)$  from  $a$  to  $b$ ,  $a < b$ ?

17. (3 points) Set up the integral for the length of  $y = x^2$  from  $x = 0$  to  $x = 1$ .

**18.** (3 points) Set up the integral for the solid of revolution for the area between  $y = x$  and  $y = x^2$  between  $x = 0$  and  $x = 1$  when it is rotated about the  $x$ -axis.

**19.** (3 points) Set up the integral for the solid of revolution for the area between  $y = x$  and  $y = x^2$  between  $x = 0$  and  $x = 1$  when it is rotated about the line  $x = -1$ .

20. (3 points) If your speed is given by  $t^3 - 1$ , how far do you go from time 1 to time 2?