## Lecture Questions II: 110.302 Differential Equations

Professor Richard Brown

Mathematics Department

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## Question 1

In the Variation of Parameters Method for finding a particular solution to a nonhomogeneous, second-order linear ODE L[y] = g(t), determine which one of the following is a true statement:

- A. The method only works when g(t) has a certain type (a sum of products of exponentials, sines or cosines and polynomials.)
- B. The resulting system in the method,

$$u'_1y_1 + u'_2y_2 = 0, \quad u'_1y'_1 + u'_2y'_2 = g(t),$$

where  $y_1(t)$  and  $y_2(t)$  comprise the fundamental set of homogeneous solutions, may be inconsistent. In this case,  $Y(t) = u_1y_1 + u_2y_2$  would not exist.

- C. It is possible for one of the two of  $u_1(t)$  and  $u_2(t)$  to be a constant as long as the other is not.
- D. One must check the Wronskian to see if Y(t) is actually independent of  $y_1$  and  $y_2$ .
- E. None of the previous statements is true.

## Question 2

Let

$$ay'' + by' + cy = 0, \quad y(t_0) = y_0, \quad y'(t_0) = y'_0$$

be a homogeneous, second-order, linear IVP with constant coefficients. If a,b,c>0, what can we say about the long term behavior of the solutions?

- A. Solutions exist and are uniquely defined for all  $t \in \mathbb{R}$ , and tend to either  $\infty$  or  $-\infty$  as  $t \to \infty$ .
- B. Solutions exist and are uniquely defined for all  $t \in \mathbb{R}$ , and all tend to 0 as  $t \to \infty$ .
- C. Solutions exist and are uniquely defined only for certain choices of a, b, and c, and where these solutions tend to depends on the initial data.
- D. Solutions exist and are uniquely defined always, but there is not enough information to determine where solutions go.
- E. Not enough information available to determine whether solutions exist and/or are uniquely defined.

## Question 3

Determine the truth of the following two statements about the Wronskian determinant of any two solutions to y'' + p(t)y' + q(t)y = 0:

- (1) The Wronskian can be used to determine precisely where solutions to the ODE exist and are unique.
- (2) If one solution is already known, one can use the Wronskian determinant to construct another independent solution.
- A. Both are true.
- B. (1) is true and (2) is false.
- C. (1) is false and (2) is true.
- D. Both are false.

