## Mathematic 405, Fall 2015: Assignment #6

## Due: Wednesday, April 1st

*Instructions:* Please ensure that your answers are legible. Also make sure that sufficient steps are shown. Page numbers refer to the course text.

**Problem #1.** Let I=(a,b) be an interval. Suppose that  $f:I\to R$  is differentable. Show that for any compact interval  $I_\delta\subset I$  with  $I_\delta=[x_0-\delta,x_0+\delta]$ , one has

- a)  $f(I_{\delta})$  is a compact interval.
- b)  $|f(I_{\delta})| |f'(x_0)||I_{\delta}| = |f(I_{\delta})| 2|f'(x_0)|\delta = o(\delta), \delta \to 0$ . Here |I| means the length of a compact interval I, so  $|I_{\delta}| = 2\delta$ . That is,  $|f'(x_0)|$  measures the extent to which f distorts length near  $x_0$ .
- c) (Optional) Give a "geometric" interpretation of the chain rule using the above observation.

**Problem #2.** p. 163 # 6

**Problem #3.** p. 163 # 8

**Problem #4.** p. 163 # 13

**Problem #5.** p. 176 # 1

**Problem #6.** p. 176 # 4

**Problem #7.** p. 176 # 10

**Problem #8.** p. 192 # 1