## ERRATA

Abstract Algebra, Third Edition<br>by D. Dummit and R. Foote<br>(most recently revised on June 26, 2006)

These are errata for the Third Edition of the book. Errata from previous editions have been fixed in this edition so users of this edition do not need to refer to errata files for the Second Edition (on this web site). Individuals using the Second Edition, however, must make corrections from this list as well as those in the Second Edition errata files (except for corrections to text only needed in the Third Edition; for such text no reference to Second Edition page numbers is given below). Some of these corrections have already been incorporated into recent printings of the Third Edition.

## page 31 , The group $\mathrm{S}_{3}$ table

last line missing
add: $\sigma_{6}(1)=3, \sigma_{6}(2)=1, \sigma_{6}(3)=2 \quad \left\lvert\, \quad\left(\begin{array}{ll}1 & 3\end{array}\right)\right.$
page 33, Exercise 10, line 2 (2 ${ }^{\text {nd }}$ Edition p. 33, Exercise 10)
from: its least residue $\bmod m$ when $k+i>m$
$t o$ : its least positive residue $\bmod m$
page 34, line 1 of Definition (2 ${ }^{\text {nd }}$ Edition p. 34, line 1 of Definition)
from: two binary operations
to: two commutative binary operations
page 39, Example 2, line - 4
from: $b a=a b^{-1}$
$t o: b a=a^{-1} b$
page 45, Exercise 22 (2 ${ }^{\text {nd }}$ Edition p. 46, Exercise 22)
from: is isomorphic to a subgroup (cf. Exercise 26 of Section 1) of $S_{4}$ to: is isomorphic to $S_{4}$
page 51, line - 1 ( $2^{\text {nd }}$ Edition p. 52, line -1)
from: see Exercise 1 in Section 1.7
to: see Exercise 4(b) in Section 1.7
page 71, Exercise 5 (2 ${ }^{\text {nd }}$ Edition p. 72, Exercise 5)
from: there are 16 such elements $x$
to: there are 8 such elements $x$
page 84, line 11 of Example 2 ( $2^{\text {nd }}$ Edition p. 85, line 11 of Example 2)
from: By Proposition 2.6
to: By Theorem 2.7(1)
page 84, line -6 of Example 2 (2 ${ }^{\text {nd }}$ Edition p. 85, line -6 of Example 2)
from: By Proposition 2.5
to: By Theorem 2.7(3)
page 98, Figure 6
$a d d$ : hatch marks to upper right and lower left lines of the central diamond (to indicate $A B / B \cong$ $A / A \cap B)$.
page 114, line 3 in Proof of Proposition 2 ( $2^{\text {nd }}$ Edition p. 116, line 3 of Proof)
from: $b \in G$
to: $g \in G$
page 132, Exercise 33, line -1 ( $2^{\text {nd }}$ Edition p. 134, line -1 of Exercise 33)
from: See Exercises 6 and 7 in Section 1.3
to: See Exercises 16 and 17 in Section 1.3
page 132, Exercise 36(c) (2 ${ }^{\text {nd }}$ Edition p. 135, Exercise 36(c))
from: $g$ and $h$ lie in the center of $G$
to: $g$ and $h$ lie in the center of $G$ and $g=h^{-1}$
page 139, Definition (1) (2 ${ }^{\text {nd }}$ Edition p. 141, Definition (1))
from: A group of order $p^{\alpha}$ for some $\alpha \geq 1$
to: A group of order $p^{\alpha}$ for some $\alpha \geq 0$
page 148, Exercise 47(i) (2 ${ }^{\text {nd }}$ Edition p. 151, Exercise 47(i))
from: that has some prime divisor $p$ such that $n_{p}$ is not forced to be 1
to: for each prime divisor $p$ of $n$ the corresponding $n_{p}$ is not forced to be 1
page 149, Exercise 54, line 4 (2 ${ }^{\text {nd }}$ Edition p. 151, line 4 of Exercise 54)
from: $G / N$ acts as automorphisms of $N$
to: $G / C_{G}(N)$ acts as automorphisms of $N$
page 151, Exercise 6, line -2 (2 ${ }^{\text {nd }}$ Edition p. 153, line - 2 of Exercise 6)
from: every pair of elements of $D$ lie in a finite simple subgroup of $D$
to: every pair of elements of $A$ lie in a finite simple subgroup of $A$
page 194, Theorem 8, line 4 ( $2^{\text {nd }}$ Edition p. 196, Theorem 8, line 4)
from: $Z_{i}(G) \leq G^{c-i-1} \leq Z_{i+1}(G)$ for all $i \in\{0,1, \ldots, c-1\}$.
to: $G^{c-i} \leq Z_{i}(G)$ for all $i \in\{0,1, \ldots, c\}$.
page 209, Proposition 14(1)
from: $n_{3}=7$
to: $n_{3}=28$
page 216, line 4 after displayed steps (1) and (2) (2 ${ }^{\text {nd }}$ Edition p. 217, line -3 )
from: are equal if and only if $n=m$ and $\delta_{i}=\epsilon_{i}, 1 \leq i \leq n$
to: are equal if and only if $n=m, r_{i}=s_{i}$ and $\delta_{i}=\epsilon_{i}, 1 \leq i \leq n$
page 260, Exercise 40(iii) (2 ${ }^{\text {nd }}$ Edition p. 261, Exercise 40(iii))
from: $R / \eta(R)$
to: $R / \mathfrak{N}(R)$
page 282, second display ( $2^{\text {nd }}$ Edition p. 283, second display)
from: $0<N\left(\frac{\alpha}{\beta} s-t\right)=\frac{(a y-19 b x-c q)^{2}+19(a x+b y+c z)^{2}}{c^{2}} \leq \frac{1}{4}+\frac{19}{c^{2}}$
and so $(*)$ is satisfied with this $s$ and $t$ provided $c \geq 5$.
to: $0<N\left(\frac{\alpha}{\beta} s-t\right)=\frac{(a y-19 b x-c q)^{2}+19(a x+b y+c z)^{2}}{c^{2}}=\frac{r^{2}+19}{c^{2}} \leq \frac{1}{4}+\frac{19}{c^{2}}$
and so $(*)$ is satisfied with this $s$ and $t$ provided $c \geq 5$ (note $r^{2}+19 \leq 23$ when $c=5$ ).
bigskippage 323, line -6
from: among the differences $S\left(g_{i}, g_{j}\right)$
to: among the remainders of the differences $S\left(g_{i}, g_{j}\right)$
page 332, Exercise 16, line 3
from: $\left(L T\left(g_{1}\right), \ldots, L T\left(g_{m}\right), L T\left(S\left(g_{i}, g_{j}\right)\right)\right.$ is strictly larger than the ideal $\left(L T\left(g_{1}\right), \ldots, L T\left(g_{m}\right)\right)$. Conclude that the algorithm ...
$t o:\left(L T\left(g_{1}\right), \ldots, L T\left(g_{m}\right), L T(r)\right)$ is strictly larger than the ideal $\left(L T\left(g_{1}\right), \ldots, L T\left(g_{m}\right)\right)$, where $S\left(g_{i}, g_{j}\right) \equiv r \bmod G$. Deduce that the algorithm ...
page 334, Exercise 43(a)
from: Use Exercise 30
to: Use Exercise 39
page 334, Exercise 43(b)
from: Use Exercise 33(a)
to: Use Exercise 42(a)
page 334, line 3 of Exercise 43(c)
from: ideal defined in Exercise 32, to: ideal quotient (cf. Exercise 41),
page 350, line 2 of Exercise 4 ( $2^{\text {nd }}$ Edition p. 331, Exercise 4)
from: $\varphi(\bar{k})=k a$
$t o: \varphi_{a}(\bar{k})=k a$
page 372, Corollary 16(2), top line of commutative diagram
from: $M \times \cdots \times M_{n} \xrightarrow{\iota} M \otimes \cdots \otimes M_{n}$
to: $M_{1} \times \cdots \times M_{n} \xrightarrow{\iota} M_{1} \otimes \cdots \otimes M_{n}$
page 374, line 2 of second Remark (2 ${ }^{\text {nd }}$ Edition p. 355 line 2)
from: Section 11.6
to: Section 11.5
page 385, title of subsection following Proposition 26
from: Modules and $\operatorname{Hom}_{R}(D,-)$
to: Projective Modules and $\operatorname{Hom}_{R}(D,-)$
page 396, line - 2 above Proposition 36 ( $2^{\text {nd }}$ Edition p. 376)
from: Exercises 18 and 19
to: Exercises 19 and 20
page 398, Proof of Theorem 38 ( $2^{\text {nd }}$ Edition p. 378)
from: Exercises 15 to 17
to: Exercises 15 and 16
page 399, line 8 ( $2^{\text {nd }}$ Edition p. 379, line 22)
from: The map $1 \otimes \varphi$ is not in general injective
$t o$ : The map $1 \otimes \psi$ is not in general injective
page 401, line 2 of Example 1 ( $2^{\text {nd }}$ Edition p. 381, line 2 of Example 1 )
from: $\mathbb{Z} / 2 \mathbb{Z}$ not a flat module to: $\mathbb{Z} / 2 \mathbb{Z}$ is not a flat module
page 403, Exercise 1(d) (2 ${ }^{\text {nd }}$ Edition p. 383, Exercise 1(d))
from: if $\beta$ is injective, $\alpha$ and $\gamma$ are surjective, then $\gamma$ is injective to: if $\beta$ is injective, $\alpha$ and $\varphi$ are surjective, then $\gamma$ is injective
page 405, Exercise 15 ( $2^{\text {nd }}$ Edition p. 385, Exercise 115)
change exercise to:
Let $M$ be a left $\mathbb{Z}$-module and let $R$ be a ring with 1 .
(a) Show that $\operatorname{Hom}_{\mathbb{Z}}(R, M)$ is a left $R$-module under the action $(r \varphi)\left(r^{\prime}\right)=\varphi\left(r^{\prime} r\right)$ (see Exercise 10).
(b) Suppose that $0 \rightarrow A \xrightarrow{\psi} B$ is an exact sequence of $R$-modules. Prove that if every $\mathbb{Z}$-module homomorphism $f$ from $A$ to $M$ lifts to a $\mathbb{Z}$-module homomorphism $F$ from $B$ to $M$ with $f=F \circ \psi$, then every $R$-module homomorphism $f^{\prime}$ from $A$ to $\operatorname{Hom}_{\mathbb{Z}}(R, M)$ lifts to an $R$-module homomorphism $F^{\prime}$ from $B$ to $\operatorname{Hom}_{\mathbb{Z}}(R, M)$ with $f^{\prime}=F^{\prime} \circ \psi$. [Given $f^{\prime}$, show that $f(a)=f^{\prime}(a)\left(1_{R}\right)$ defines a $\mathbb{Z}$-module homomorphism of $A$ to $M$. If $F$ is the associated lift of $f$ to $B$, show that $F^{\prime}(b)(r)=F(r b)$ defines an $R$-module homomorphism from $B$ to $\operatorname{Hom}_{\mathbb{Z}}(R, M)$ that lifts $f^{\prime}$.]
(c) Prove that if $Q$ is an injective $\mathbb{Z}$-module then $\operatorname{Hom}_{\mathbb{Z}}(R, Q)$ is an injective $R$-module.
page 423, line 3 of Exercise 9 ( $2^{\text {nd }}$ Edition p. 403, Exercise 9)
from: If $\left.\varphi\right|_{W}$ and $\widetilde{\varphi}$ are
to: If $\left.\varphi\right|_{W}$ and $\bar{\varphi}$ are
page 426, line 2 of Exercise 21(b) (2 ${ }^{\text {nd }}$ Edition p. 406, Exercise 21(b))
from: $6 z$
$t o:+6 z$
page 433, proof of Theorem 19, line 3
from: $=E_{v}(f)+\alpha E_{g}(v)$
$t o:=E_{v}(f)+\alpha E_{v}(g)$
page 435, Exercise 1
change exercise to:
Let $V$ be a vector space over $F$ of dimension $n<\infty$. Prove that the map $\varphi \mapsto \varphi^{*}$ in Theorem 20 is a vector space isomorphism of $\operatorname{End}(V)$ with $\operatorname{End}\left(V^{*}\right)$, but is not a ring homomorphism when $n>1$. Exhibit an $F$-algebra isomorphism from $\operatorname{End}(V)$ to $\operatorname{End}\left(V^{*}\right)$.
page 442, line -8 ( $2^{\text {nd }}$ Edition p. 422, line -8)
from: $\varphi: M \rightarrow A$ is an $R$-algebra
to: $\varphi: M \rightarrow A$ is an $R$-module
page 566, Example 7, first line after second display
from: we see that $\sigma_{p}^{p^{n}}=1$
$t o$ : we see that $\sigma_{p}^{n}=1$
page 584, Exercise 24 ( $2^{\text {nd }}$ Edition p. 564, Exercise 24)
change exercise to:
Prove that the rational solutions $a, b \in \mathbb{Q}$ of Pythagoras' equation $a^{2}+b^{2}=1$ are of the form $a=\frac{s^{2}-t^{2}}{s^{2}+t^{2}}$ and $b=\frac{2 s t}{s^{2}+t^{2}}$ for some $s, t \in \mathbb{Q}$. Deduce that any right triangle with integer sides has sides of lengths $\left(\left(m^{2}-n^{2}\right) d, 2 m n d,\left(m^{2}+n^{2}\right) d\right.$ ) for some integers $m, n, d$. [Note that $a^{2}+b^{2}=1$ is equivalent to $\mathrm{N}_{\mathbb{Q}(i) / \mathbb{Q}}(a+i b)=1$, then use Hilbert's Theorem 90 above with $\beta=s+i t$.]
page 585, Exercise 29(b) (2 ${ }^{\text {nd }}$ Edition p. 565, Exercise 29(b))
from: Prove that the element $t=$
$t o:$ Prove that the element $s=$
page 585, Exercise 29(c) (2 ${ }^{\text {nd }}$ Edition p. 565, Exercise 29(c))
from: Prove that $k(t)$
$t o$ : Prove that $k(s)$
page 654, Exercise 16 (2 ${ }^{\text {nd }}$ Edition p. 635, Exercise 16)
from: Prove that $F$ does not contain all quadratic extensions of $\mathbb{Q}$.
to: Prove that $F$ does contain all quadratic extensions of $\mathbb{Q}$. [One way is to consider the polynomials $x^{3}+3 a x+2 a$ for $a \in \mathbb{Z}^{+}$.]
page 670, line 2 of Exercise 34 ( $2^{\text {nd }}$ Edition p. 648, Exercise 34)
from: $\operatorname{Ass}_{R}(N) \subseteq \operatorname{Ass}_{R}(M)$
$t o: \operatorname{Ass}_{R}(L) \subseteq \operatorname{Ass}_{R}(M)$
page 707, line 2 of Corollary $37(1)$ ( $2^{\text {nd }}$ Edition p. 678, Corollary 29(1))
from: if and only if $D$ contains no zero divisors of $R$
to: if and only if $D$ contains no zero divisors or zero
page 721, line 4 after commutative diagram (2 ${ }^{\text {nd }}$ Edition p. 688, line 2)
$\begin{aligned} \text { from: By Proposition 38(1) } & {\left[\mathbf{2}^{\text {nd }} \text { Edition: By Proposition 30(1)] }\right.} \\ \text { to: By Proposition 46(1) } & {\left[\mathbf{2}^{\text {nd }} \text { Edition: By Proposition } 36(1)\right] }\end{aligned}$
page 728, Exercise 21, line 1
from: Suppose $\varphi: R \rightarrow S$ is a ring homomorphism
to: Suppose $\varphi: R \rightarrow S$ is a ring homomorphism with $\varphi\left(1_{R}\right)=1_{S}$
page 754, line 2 of Exercise 8 ( $2^{\text {nd }}$ Edition p. 720, Exercise 8)
from: Observe the
to: Observe that
page 781, bottom row of diagram (17.9) ( $2^{\text {nd }}$ Edition p. 748, diagram (17.9))
from: $0 \longrightarrow \operatorname{Hom}_{R}(A, D) \longrightarrow$ to: $0 \longrightarrow \operatorname{Hom}_{R}\left(A^{\prime}, D\right) \longrightarrow$
page 793, line 4 of Exercise 11(c) (2 ${ }^{\text {nd }}$ Edition p. 760, Exercise 11(c))
from: projection maps $I \rightarrow I_{i}$
to: projection maps $I \rightarrow I / I_{i}$
page 794, Exercise 17 (2 ${ }^{\text {nd }}$ Edition p. 761, Exercise 17)
from: for any abelian group $A$
to: for any abelian group $B$
page 800, line -7 ( $\mathbf{2}^{\text {nd }}$ Edition p. 766, line -7)
from: $H^{n}(G, A) \cong E x t^{n}(\mathbb{Z}, A)$
to: $H^{n}(G, A) \cong E x t_{\mathbb{Z} G}^{n}(\mathbb{Z}, A)$
page 801, line 4 ( $\mathbf{2}^{\text {nd }}$ Edition p. 767, line 4)
from: 1 if $n$ is odd $t o: a$ if $n$ is odd
page 812, Exercise 18(a) (2 ${ }^{\text {nd }}$ Edition p. 778, Exercise 18(a))
from: from $\mathbb{Z} /(m / d) \mathbb{Z}$ to $\mathbb{Z} / m \mathbb{Z}$ if $n$ is odd, and from 0 to 0 if $n$ is even, $n \geq 2$, to: from 0 to 0 if $n$ is odd, and from $\mathbb{Z} /(m / d) \mathbb{Z}$ to $\mathbb{Z} / m \mathbb{Z}$ if $n$ is even, $n \geq 2$,
page 813, line 3 of Exercise 19 ( $2^{\text {nd }}$ Edition p. 779, Exercise 19)
from: p-primary component of $H^{1}(G, A)$
to: p-primary component of $H^{n}(G, A)$
page 815, line 2 of Proposition 30 ( $2^{\text {nd }}$ Edition p. 781)
from: group homomorphisms from $G$ to $H$
to: group homomorphisms from $G$ to $A$
page 816, line - 13 ( $2^{\text {nd }}$ Edition p. 782, line -13)
from: bijection between the elements of
to: bijection between the cyclic subgroups of order dividing $n$ of
page 832, lines -10 and -14 ( $2^{\text {nd }}$ Edition p. 798, lines -6 and -10 )
from: $L$
to: $K$
page 853, line 4 of Exercise 17 ( $2^{\text {nd }}$ Edition p. 819, Exercise 17)
from: Your proof ...
to: Your proof that $\varphi$ has degree 1 should also work for infinite abelian groups when $\varphi$ has finite degree.
page 869, line -6 (2 ${ }^{\text {nd }}$ Edition p. 835, line -6)
from: the isotypic components of $G$ to: the isotypic components of $M$
page 885, Exercise 8 (2 ${ }^{\text {nd }}$ Edition p. 851, Exercise 8)
from: This table contains nonreal entries.
to: This table contains irrational entries.
page 893, line 4 ( $2^{\text {nd }}$ Edition p. 859, line 4)
from: a proper, nontrivial subgroup of $G$ to: a proper, nontrivial normal subgroup of $G$
page 899, line 1 of item (3) (2 ${ }^{\text {nd }}$ Edition p. 865)
from: let $Q_{3}$ be a Sylow 11-subgroup of $G$ to: let $Q_{3}$ be a Sylow 13-subgroup of $G$
page 907, Exercise 1(a) (2 ${ }^{\text {nd }}$ Edition p. 873, Exercise 1(a))
from: a 3-tuple in $A \times A \times A$ maps to an ordered pair in $A \times A$ to: an ordered pair in $A \times A$ maps to a 3 -tuple in $A \times A \times A$
page 912, line 6 ( $2^{\text {nd }}$ Edition p. 878, line 6)
from: if $A \neq B$ or $C \neq D$
to: if $A \neq C$ or $B \neq D$

