## Math 109, Fall 2018 Midterm 2

## Name: Section:

## **Requirements:**

This exam should be completed in **45 minutes**.

■Books, notes, calculators, computers, discussion and collaboration are not allowed.

■Do all of your work in this exam booklet.

■Simplify all answers as far as possible.

■Solutions without proper justification will receive no credit.

Problem	Points	Score
1	15	
2	15	
3	20	
4	20	
5	10	
6	20	
Total	100	

**Problem 1. (15')** Find the area of the region that is bounded by the polar curve  $r = \sin \theta$  and lies in the sector  $\frac{\pi}{6} \le \theta \le \frac{\pi}{3}$ .

**Problem 2. (15')** Determine whether the following improper integral converges or diverges. If it converges, compute it.

$$\int_0^1 \frac{1}{x^2 - 4x + 3} dx.$$

**Problem 3. (20')** Determine whether the following improper integral converges or diverges. Explain it.

a) 
$$\int_{1}^{10} \frac{1}{\sqrt[5]{x-3}} dx.$$
  
b)  $\int_{10}^{\infty} \frac{1}{x^2 - 4} dx.$ 

**Problem 4. (20')** Determine whether the following sequence  $\{a_n\}_{n=1}^{\infty}$  converges or diverges. If it converges, compute the limit.

a) 
$$a_n = \frac{\ln(n^2 + 2)}{\ln(3n)}.$$

b) 
$$a_n = \frac{(-1)^n}{2\sqrt{n}}.$$

**Problem 5.** (10') Determine whether the series  $\sum_{n=1}^{\infty} \cos \frac{1}{n^3}$  converges or diverges. Explain it.

**Problem 6. (20')** Determine whether the series converges or diverges. If it converges, compute it.

a) 
$$\sum_{n=0}^{\infty} \frac{2}{5^{n+1}}$$

b) 
$$\sum_{n=0}^{\infty} (\frac{3}{2})^n$$